

# Development of VIcarious Calibration tool for MWI and ICI using RadioSoundings (VICIRS)

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**Objective**: develop a vicarious calibration and validation (Cal/Val) tool to compare MWI and ICI observations against radiosoundings.

Vicarious calibration: post-launch calibration based on targets imaged near-coincidently by the sensor to be calibrated and by one or more well-calibrated sensors (from satellites, aircraft, balloon or ground).

MicroWave Imager (MWI) and Ice Cloud Imager (ICI) are conical-scanning microwave radiometers that will fly from 2025 onward aboard the 2nd generation European Polar Satellites (METOP-SG-B).





### MWI

 26 channels centred at 18 frequency bands (from 18 to 183 GHz)

#### Main applications:

- cloud/precipitation in support of NWP
- ocean surface (wind speed, sea ice)
- MW legacy in support of long-term climate records

Channel	Frequency (GHz)	Bandwidt h(MHz)	NEDT (K)	Radiometric Bias (K)	Polarization	Footprint Size at 3dB (km)
MWI-I	18.7	200	0.8	1.0	V, H	50
MWI-2	23.8	400	0.7	1.0	V, H	50
MWI-3	31.4	200	0.9	1.0	V, H	30
MWI-4	50.3	180	1.1	1.0	V, H	30
MWI-5	52.7	180	1.1	1.0	V, H	30
MWI-6	53.24	400	1.1	1.0	V, H	30
MWI-7	53.750	400	1.1	1.0	V, H	30
MWI-8	89.0	4000	1.1	1.0	V, H	10
MWI-9	118.7503±3.20	2x500	1.3	1.0	V	10
MWI-10	118.7503±2.10	2x400	1.3	1.0	V	10
MWI-II	118.7503±1.40	2x400	1.3	1.0	V	10
<b>MWI-12</b>	118.7503±1.20	2x400	1.3	1.0	V	10
MWI-13	165.5±0.75	2x1350	1.2	1.0	V	10
<b>MWI-14</b>	183.31±7.0	2x2000	1.3	1.0	V	10
MWI-15	183.31±6.1	2x1500	1.2	1.0	V	10
MWI-16	183.31±4.9	2×1500	1.2	1.0	V	10
MWI-17	183.31±3.4	2×1500	1.2	1.0	V	10
<b>MWI-18</b>	183.31±2.0	2×1500	1.3	1.0	V	10

#### Incidence angles within 53°±2°

Observations acquired  $\pm 65^{\circ}$  in azimuth in the fore view (about 1700 km swath)

Footprints overlap  $\geq 20\%$ .

Spatial sampling: ~9 km along track ,~2.5 km across track.



## ICI

 I3 channels centred at II frequency bands (from 183 to 664 GHz)

#### Main applications:

- ice cloud products for climate monitoring
- information on non-precipitating ice

Channel	Frequency (GHz)	Bandwidth (MHz)	NEDT (K)	Radiometr ic Bias (K)	Polarization	Footprint Size at 3dB (km)
ICI-I	183.31±7.0	2x2000	0.8	I	V	16
ICI-2	183.31±3.4	2x1500	0.8	I	V	16
ICI-3	183.31±2.0	2x1500	0.8	I	V	16
ICI-4	243.2±2.5	2x3000	0.7	1.5	V, H	16
ICI-5	325.15±9.5	2x3000	1.2	1.5	V	16
ICI-6	325.15±3.5	2x2400	1.3	1.5	V	16
ICI-7	325.15±1.5	2x1600	1.5	1.5	V	16
ICI-8	448±7.2	2x3000	1.4	1.5	V	16
ICI-9	448±3.0	2x2000	1.6	1.5	V	16
ICI-10	448±1.4	2x1200	2.0	1.5	V	16
ICI-II	664±4.2	2×5000	1.6	1.5	V, H	16

Incidence angles within 53°±2°

Observations acquired  $\pm 65^{\circ}$  in azimuth in the fore view (about 1700 km swath)

Footprints overlap  $\geq$ 40%.

Spatial sampling: ~9 km along track ,~2.5 km across track.



Why vicarious calibration against radiosoundings?

Crucial for unprecedented channels (ICI-4 : ICI-11), (MWI-9 : MWI-12)\*

Processed with RTM to compute simulated observations (Brightness Temperature BT)

How to characterize the uncertainty of simulated BT?



\* Except for TROPICS



## Propagating radiosounding uncertainties



What radiosonde archive?



Seidel et al., 2009



# **RADIOSONDE OBSERVATIONS**

#### Global Climate Observing System (GCOS) Reference Upper-Air Network (GRUAN)

- homogeneous and fully traceable with quantified uncertainties
- 31 sites, 14 of which have been GRUAN certified
- 23 with active data streams (other under implementation)



GCOS Reference Upper-Air Network



# RADIOSONDE OBSERVATIONS

#### Copernicus Climate Change Service (C3S), Radiosounding HARMonization (RHARM)

- bias-adjusted radiosounding observations from the Integrated Global Radiosonde Archive (IGRA)
- estimated uncertainties (building on GRUAN expertise and intercomparison data)
- 700 sites (+ ships)



(Madonna et al., 2022)



# **ROADMAP TO VICIRS**

VIcarious Calibration and validation tool to compare MWI and ICI observations to RadioSoundings VICIRS



# **VICIRS** INTRODUCTION TO VICIRS TOOL: OVERVIEW







## VICIRS TOOL FLOWCHART

Step \*: Input/output management, decision loop and plotting/reporting management

STEP I: match-ups search; data download

STEP II: RS quality check; RS and NWP clear-sky check; RS AMD test

STEP III: TA types extraction, TA clear-sky check and emissivity screening

**STEP IV: BT simulation** 

Step V: bias and uncertainties analysis

Step VI: Multisource Correlative Methodology analysis (MCM)



# FIRST PHASE: DATA COLLECTION

## Flexible input

- radiosonde archive: —
- temporal range:
- temporal distance: \_\_\_\_

- GRUAN & RHARM
  - aaaa-mm-dd hh:mm (start) to aaaa-mm-dd hh:mm (end) -15'  $\leq \Delta t \leq 45$ '
  - -1 hour  $\leq \Delta t \leq 1$  hour -3 hours  $\leq \Delta t \leq 3$  hours

- spatial range:
- land fraction (LF):
- Multisource:

lat North/long West/lat South/long East
 maximum value of MWI/ICI FOV (100)
 Dedicated RS & NWP



# **RS AND NWP CHECK**

## Is RS useful for calibration process?

## **RS** quality check

- number of pressure levels;
- pressure minimum value;
- air mass displacement (Buehler et al. 2004);
- clear-sky test (Zhang et al. 2010)

## Is NWP useful for calibration process?

## **NWP** quality check

• clear-sky test





# **VICIRS TOOL: TA ANALYSIS**

29.0<sup>°</sup> N

28.5<sup>°</sup> N

28.0<sup>°</sup> N

Target Area	(TA) analysis	
	I: circular TA	29.0
	2: circular TA (inverse distance weight)	28.
TA types	3: circular TA (inverse squared-distance weight)	28.0
	4: RS-driven TA	27 5
	5: RS-driven TA (3x3)	27.5

$$BT_{TA} = \sum_{i=1}^{N} BT_{i} \cdot \lambda_{i,j} \qquad \lambda_{i,j} = \frac{d_{0i}^{-j}}{\sum_{i=1}^{N} d_{0i}^{-j}}$$













278

276

274

272

Clear sky test ٠



# **CLOUD SCREENING**

	183 GHz	89 Ghz	l 65 Ghz	664v GHz
MWI	Buehler et al, 2007 Hong et al, 2005	over land: Yaping et al, 2008 over sea: Gong and Wu, 2017	Yaping et al, 2008	
ΙCΙ	Clain et al, 2005			Gong and Wu, 2017

MWI/ICI level 1B data orbit 4656 (20070912102225 to 20070912120114) simulated from 2007-09-12 10:00 UTC ERA-5 data

MSG-SEVIRI image acquired on 2007-09-12 10:15 UTC















## RADIATIVE TRANSFER MODEL

## **GRUAN Processor v6.3.b.0.1**

#### **GRUAN Processor v6.3**

- developed by Carminati et al. (2019) to process GRUAN RS and propagate RS uncertainties
  - based on RTTOV and RadSim (from NWP-SAF)

#### **GRUAN Processor v6.3.b.0.**

- upgraded to work with
  - latest RTTOV (vI 3.2)
  - latest GRUAN RS (RS41)
  - RHARM RS
  - latest emissivity model



# **BT SIMULATION**

#### BT simulation from GRUAN RS



#### BT simulation from RHARM RS



 $BT_{RS} = LF_{TA} \cdot BT_{RS} l + (1 - LF_{TA}) \cdot BT_{RS} s$ 

 $uBT_{RS} = \sqrt{LF_{TA}(i,j)^2 \cdot uBT_{RS} - l(i)^2 + (1 - LF_{TA})^2 \cdot uBT_{RS} - s^2)}$ 



## UNCERTAINTY ANALYSIS

- Uncertainty model diagram
- Review of uncertainty sources
- Knowledge gap analysis





## UNCERTAINTY MODEL DIAGRAM

π.





## **REVIEW OF UNCERTAINTY SOURCES**

- Instrument noise
  - Calibration
  - ΝΕΔΤ
- Radiosonde uncertainty
  - GRUAN
  - RHARM
- Radiative transfer model (RTM) uncertainty
  - Absorption model



Gallucci et al, ACPD, egusphere-2023-3160



- Spatial colocation
- Geolocation
- RTM contribution of:
  - Surface emissivity model
  - Atmospheric model
    - Optimization
    - Discretization



#### **Spatial colocation**

- Target area (TA) approach<sup>1</sup>
- u<sub>BT</sub> = STD(BT<sub>TA</sub>)
- Circular, RS-driven



17.0°W 16.5°W 16.0°W 15.5°W



<sup>1</sup>Buehler et al, 2004; Moradi et al, 2010



#### Geolocation

- Analysis based on 183-GHz channels<sup>1</sup>
  - Average geolocation error ~6 km
  - ~113 km<sup>2</sup>
- Same order of magnitude of MWI/ICI IFOV distances
  - ~2x9 km (cross-track x along-track)
- u<sub>GEOL</sub> = STD(BT<sub>(3x5-IFOV)</sub>)
  - ~144 km<sup>2</sup>
  - Based on simulated MWI & ICI lev1b data





<sup>1</sup>Papa et al, 2021 doi: 10.1109/TGRS.2020.3024677



#### **RTM contribution of surface emissivity**

- RTM perturbation
- According to land/sea surface uncertainty estimate<sup>1,2</sup>
  - $\sigma_{\rm e}$  = 0.05 (over land)
  - $\sigma_{\rm e}$  = 0.018 (over ocean)





<sup>1</sup>Wang et al. 2017, doi: 10.1175/JTECH-D-16-0188.1 <sup>2</sup>Kilic et al. 2023, doi:





#### **RTM contribution of atmospheric model**

- RTM optimization
  - Fast parameterized (RTTOV) vs. accurate line-by-line (LBL)
  - RTTOV vs LBL BT<sup>1</sup>
    - diverse 83 profile set and six zenith angles
- Vertical interpolation<sup>2</sup>
  - Discrete levels vs. dense atmosphere
  - N<sub>user lev</sub> > N<sub>coef lev</sub>
  - Adapted to MWI/ICI from ATMS channels





<sup>1</sup>Hocking, NWPSAF, <u>LBL vs RTTOV v13</u> <sup>2</sup>Hocking 2014, NWPSAF Techl Rep No: 590



## TOTAL UNCERTAINTY

Total uncertainty comes from all the contributions of estimated sources

$$u_{all} = \sqrt{\sum u_i^2} = \sqrt{u_{i_{OBS}}^2 + u_{i_{SIM}}^2 + u_{i_{COL}}^2}$$



## MULTISOURCE CORRELATIVE METHODOLOGY ANALYSIS Introduction

#### GOAL of MCMA methodology

 $\circ$  Provide an error variance estimate ( $\sigma^2{}_{\it {\cal E}}$  ) of three sources of BT (e.g. RS, SAT, NWP)

Provide an estimate of calibration parameters (bias:
 *b<sub>i</sub>* and scaling *a<sub>i</sub>*) of two out of three sources (eg. sources 2 and 3)

#### Main requirements for MCMA

 $\odot$  Each source,  $\textit{BT}_i$  , has a linear dependence with the unobserved truth BT

 $\circ$  The tree sources of  $BT_i$  are space-time collocated (i.e. they are originated by the same quantity BT)

• The <u>ERRORS</u> ( $\mathcal{E}_i$ ) are independent to each other. (IF NOT, some extra errors have to be considered in the final estimation of  $\sigma^2_{\mathcal{E}_i}$ )

• Plus, other requirements which are typically verified...





## MULTISOURCE CORRELATIVE METHODOLOGY ANALYSIS EXPERIMENT SET UP

Error varia	nces $\sigma_{\varepsilon}^2$	$f_i^2$ (K <sup>2</sup> )		
0.12	0.5 <sup>2</sup>	1.0 <sup>2</sup>	1.5 <sup>2</sup>	2

- 5×5×5 =125 different combinations of the error triplets ε<sub>1</sub>, ε<sub>2</sub>, ε<sub>3</sub>
- For each error triplet configuration, a variable N<sub>s</sub> samples of BT are considered

Calibration parameters used to generate input triplets									
Cases	label	$a_1$	$a_2$	$a_3$	$b_1$	$b_2$	$b_3$	$ ho_{12}$	
Ideal case	(ID)		I	I	0	0	0	0	
Inter. case	(IN)	I	1.25	0.75	0	Ι	I	0	
Worst case I	(WI)	0.75 – 1.25	1.25	0.75	0	I		0	
Worst case 2	(W2)	0.75 – 1.25	1.25	0.75	0	I	I	0.1	
Worst case 3	(W3)	0.75 – 1.25	1.25	0.75	0	I	Ι	0.3	

- Five cases (ID,IN,W1,W2,W3) are considered
- Last column indicate the degree of error correlation between system 1 and 2 to check the error tolerance to such condition



 $b_{2}, a_{2}; b_{3}, a_{3};$ 

## **MULTISOURCE CORRELATIVE METHODOLOGY ANALYSIS** <u>RESULTS:</u> $\hat{\sigma}_{\varepsilon_i}$ RETRIEVAL



calibration parameters used to generate input triplets								
Cases	label	$a_1$	$a_2$	$a_3$	$b_1$	$b_2$	$b_3$	$ ho_{12}$
Ideal case	(ID)	1	1	1	0	0	0	0
Inter. case	(IN)	1	1.25	0.75	0	1	1	0
Worst case 1	(W1)	0.75 – 1.25	1.25	0.75	0	1	1	0
Worst case 2	(W2)	0.75 – 1.25	1.25	0.75	0	1	1	0.1
Worst case 3	(W3)	0.75 - 1.25	1.25	0.75	0	1	1	0.3



- > As long as the system errors 1 & 2 are not correlated ( $\langle \varepsilon_1 \varepsilon_2 \rangle = 0$ ) there is an inverse dependence of estimated  $\hat{\sigma}_{\varepsilon_i}$  from the number of samples (*Ns*) considered (cases in the upper panel rows).
- When considering  $\langle \varepsilon_1 \varepsilon_2 \rangle \neq 0$ , errors generally increases and the dependence from *Ns* tends to vanish (lower panels).
- At worst (W3), if  $\hat{\sigma}_{\varepsilon_i}$  is estimated with a minimum of Ns =100 samples, the estimation uncertainty of MCMA is of 0.4 K RMSE.

## **MULTISOURCE CORRELATIVEMETHODOLOGY ANALYSIS** <u>RESULTS:</u> *b*<sub>i</sub> RETRIEVAL



calibration parameters used to generate input triplets								
Cases	label	$a_1$	$a_2$	$a_3$	$b_1$	$b_2$	$b_3$	$ ho_{12}$
Ideal case	(ID)	1	1	1	0	0	0	0
Inter. case	(IN)	1	1.25	0.75	0	1	1	0
Worst case 1	(W1)	0.75 – 1.25	1.25	0.75	0	1	1	0
Worst case 2	(W2)	0.75 – 1.25	1.25	0.75	0	1	1	0.1
Worst case 3	(W3)	0.75 – 1.25	1.25	0.75	0	1	1	0.3



of TC retrieval for b <sub>i</sub> (K)

RMSE (

10

The bias  $b_i$  has a very strong dependence from the number,  $N_s$ , of triplets considered and, in general, a high number of them can guarantees acceptable estimation accuracy.

E.g.  $N_s > 10^3$  triplets are needed to achieve an accuracy less than 2K for  $\hat{b}_i$  of system 3 in the worst W3 experiment.

## VICIRS MULTISOURCE CORRELATIVE METHODOLOGY ANALYSIS: <u>RESULTS:</u> a<sub>i</sub> RETRIEVAL



calibration parameters used to generate input triplets								
Cases	label	$a_1$	$a_2$	$a_3$	$b_1$	$b_2$	$b_3$	$ ho_{12}$
Ideal case	(ID)	1	1	1	0	0	0	0
Inter. case	(IN)	1	1.25	0,75	0	1	1	0
Worst case 1	(W1)	0.75 – 1.25	1.25	0.75	0	1	1	0
Worst case 2	(W2)	0.75 – 1.25	1.25	0.75	0	1	1	0.1
Worst case 3	(W3)	0.75 – 1.25	1.25	0,75	0	1	1	0.3



- RMSE of  $\hat{a}_i$  are not much sensible to the number of input triplets in the presence of miscalibrations (i.e. when worst cases are considered, bottom panels).
- In the W3 case, the RMSE is always lower than 0.5 K<sup>-1</sup> (i.e.  $\pm 13^{\circ}$  with respect to the 1:1 line in the scatterplot of the measurement  $x_i$  vs. the truth t.



- The number of input triplets play a role in the uncertainty of the final result. Less than 100 triplets risk to provide unrealistic results due to statistical fluctuations.
- The scaling parameter is estimated with an accuracy lower than  $\pm 0.5 \text{ K}^{-1}$  (worst case)
- The estimation of the bias parameter seems to be affected by large errors (<2 K, Ns>=10^3) when considering the worst case.

#### **Final Remarks**

- Caution when using MCMA .
- Better to use MCMA as confirmatory tool together with more customary approaches.



## DEMONSTRATION OF VICIRS TOOL

Testing of VICIRS tool on two datasets:

- MWI and ICI L1B simulated dataset and spatially and temporally collocated RSs from RHARM archive
  - > 2007-09-12 08:00 to 2007-09-12 12:00
  - > 2008-02-23 08:30 to 2008-02-23 10:30
     112 match-ups

- NASA Global Precipitation Measurement (GPM) Microwave Imager (GMI) observations, and spatially and temporally collocated RSs from GRUAN Archive
  - ➤ 2023-01-01 00:00 to 2023-04-30 23:59
  - > 2023-09-01 00:00 to 2023-11-30 23:59
  - 65 match-ups







## DEMONSTRATION OF VICIRS TOOL

#### SECOND PHASE: DATA QUERY

- radiometer
- radiosonde archive
- temporal range
- temporal distance
- spatial range
- target area
- land fraction range
- target area cloudy percentage
- dedicated launches;
- NWP (and option for skin temperature)
- homogeneity flag
- MCM analysis

MWI, ICI, GMI GRUAN, RHARM

aaaa-mm-dd hh:mm (start) to aaaa-mm-dd hh:mm (end)

- -15'≤  $\Delta T$  ≤45'
- -1 hour ≤  $\Delta T$  ≤1 hour
- -3 hours  $\leq \Delta T \leq$ 3 hours

spatial range; 1, 2, 3, 4, 5 [LFmin: LFmax] maximum value for cloudy percentage 0, 1 0, 1 (1,2) 0 all TAs, 1 only homogeneous TA 0=no, 1=yes



# QUERY ON MATCH-UPS: OUTPUT

#### $BT_{TA} - BT_{RS} \le k \cdot u\_all$



GMI BIAS 7. [K] - GMI GRUAN 202301010000-202311302330 -90.00 90.00 -180.00 180.00 3 1 30.0.00 1.00.000 10 O-S BIAS BIAS uncertainty O-S standard deviation -5 [X] (S-0) -10 م -15 -20 -25 -30 7 Channel 12 13 4 10 11

BIAS



Channel

weighted BIAS

- k=l (data are consistent);
- k=2 (data are in statistical agreement);
- k=3 (data are significantly different);.
- results do not agree within k=3

for all the match-ups and for all the frequencies

$$BIAS = \frac{\sum_{i=1}^{nsample} TA_RS(i,j)}{nsample}$$
$$SD_TA_RS = \sqrt{\frac{\sum_{i=1}^{nsample} (BIAS(j) - TA_RS(i,j))^2}{nsample}}$$
$$u_BIAS = \frac{SD_TA_RS}{\sqrt{nsample}}$$

for all the frequencies

$$wBIAS = \frac{\sum_{i=1}^{nsample} w_{i,j} \cdot TA_{RS}(i,j)}{\sum_{i=1}^{nsample} w_{i,j}}, \quad w_{i,j} = 1/(u_{all}(i,j))^{2}$$

$$SDw_TA_RS = \sqrt{\frac{\sum_{i=1}^{nsample} w_{i,j} \cdot (wBIAS(j) - TA_RS(i,j))^2}{\sum_{i=1}^{nsample} w_{i,j} - (\sum_{i=1}^{nsample} w_{i,j}^2 / \sum_{i=1}^{nsample} w_{i,j})}}$$
$$u_wBIAS = \sqrt{\frac{1}{\sum_{i=1}^{nsample} w_{i,j}}}$$

# **DEMONSTRATION OF VICIRS TOOL:** ICI L1B – RHARM, $LF \in [0:100]$

#### ALL DATA (UNFILTERED)

#### FILTERED (n<sub>lev,</sub> P<sub>min</sub>)



# **DEMONSTRATION OF VICIRS TOOL:** ICI L1B – RHARM, $LF \in [0:100]$

#### ALL DATA (UNFILTERED)

II2 match-ups, *Rharm Pmin*  $\in$  [10:400]*hPa*, *nlev*  $\geq$  15

#### **FILTERED** ( $n_{lev}$ , $P_{min}$ ) 10 match-ups, *Rharm Pmin* $\in$ [10: 100]*hPa*, *nlev* $\geq$ 40



# **VERIFICATION AND VALIDATION OF** VICIRS TOOL: GMI – GRUAN, $LF \in [0: 100]$

#### GMI-GRUAN 67 match-ups, temporal distance = 3



#### GMI-GRUAN 19 match-ups, temporal distance = 1

7.5 10.0 12.5 15.0 17.5

2.5 5.0



- k=3 (data are significantly different);.
- results do not agree within k=3

# VERIFICATION AND VALIDATION OF VICIRS





# SUMMARY & CONCLUSIONS

VICIRS tool for the vicarious calibration of MWI/ICI observations against radiosonde observations

- flexible
- user friendly
- GRUAN and RHARM RS
- uncertainty characterization & multisource analysis
- tested with simulated and real observations
  - MWI/ICI & GMI



# SUMMARY & CONCLUSIONS

**Current limitations** 

- RHARM v1 archive (n<sub>lev</sub> & P<sub>min</sub>)
- land fraction for GMI (not available)
- will be surpassed with RHARM v2 & MWI/ICI land fraction

Future work

- further uncertainty characterization
  - e.g., temporal collocation, NWP,...
- assess overall quality of estimated bias and accuracy vs. RS quantity and quality
- use VICIRS tool within the MWI/ICI Cal/Val activities



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# **BACK-UP SLIDES**



## VICIRS tool: Step II RS and NWP check

RS is in clear sky. The presence of cloudy layers is verified by comparing the RH values with the reference values for clear sky as determined by Zhang et al. (2010). It outputs the number of levels contaminated by low, middle and high clouds.

<b>GRUAN</b> site	POD (%)	FAR (%)	Bias	Accuracy
LAU	94	8.62	1.03	0.87
GVN	99	10.4	1.10	0.89
LIN	95	7.98	1.03	0.88
PAY	88	2.16	0.89	0.87
SNG	100	0.00	1.00	1.00

RH test (Zhang et al. 2010) vs RS-GRUAN SynopClouds Dichotomous statistical scores between cloud detection methods VICIRS MULTISOURCE CORRELATIVE METHODOLOGY ANALYSIS: EQUATIONS (1/2)

Measurement x from *i*-th source (MWR, NWP, RAOB ....) at *n*-th space-time location

 $x_i = b_i + a_i t + \varepsilon_i$   $a_i$ : calibration scaling of measuring system i - th

 $b_i$ : calibration bias of measuring system i - th

*t*: *unobserved truth* which is common to all the measuring systems

Assumptions

 $\mathcal{E}_i$ : *unknown random error* of system i - th

Assumption1 (A1). Linearity: eq. (1) holds.

<u>Assumption2 (A2)</u>:  $\varepsilon_i$  is zero average random error.

<u>Assumption3 (A3)</u>: Error orthogonality, i.e.  $\langle \varepsilon_i t \rangle = 0$ .

<u>Assumption4 (A4)</u>: Error independence i.e.:  $e_{ij} = \langle \varepsilon_i \ \varepsilon_j \rangle = 0$  with  $i \neq j$ 

<u>Assumption5 (A5)</u>: Stationarity of both t and  $x_i$ 

<u>Assumption6 (A6)</u>: the three measuring systems,  $x_i$ , i = 1, 2, 3 must observe the same quantity t.

# Outcomes Error variances

# $\begin{aligned} \hat{\sigma}_{\varepsilon_{1}}^{2} &= \sigma_{x_{1}}^{2} - \frac{C_{13}}{C_{23}}(C_{12} - e_{12}) \\ \hat{\sigma}_{\varepsilon_{2}}^{2} &= \sigma_{x_{2}}^{2} - \frac{C_{23}}{C_{13}}(C_{12} - e_{12}) \\ \hat{\sigma}_{\varepsilon_{3}}^{2} &= \sigma_{x_{3}}^{2} - C_{13} C_{23} \left(\frac{1}{C_{12} - e_{12}}\right) \end{aligned}$

#### **Correlation coefficients**

 $\hat{\rho}_{t,x1} = \frac{1}{\hat{\sigma}_{x1}} \sqrt{\frac{(C_{12} - e_{12}) C_{13}}{C_{23}}}$  $\hat{\rho}_{t,x2} = \frac{1}{\hat{\sigma}_{x2}} \sqrt{\frac{(C_{12} - e_{12}) C_{23}}{C_{13}}}$  $\hat{\rho}_{t,x3} = \frac{1}{\hat{\sigma}_{x3}} \sqrt{\frac{C_{23} C_{13}}{(C_{12} - e_{12})}}$ 

Covariance definition:

$$C_{ij} = \frac{1}{N_s - 1} \sum_{n=1}^{N_s} [(x_i(n) - \mu_{x_i})(x_j(n) - \mu_j)] = \langle (x_i - \mu_{x_i})(x_j - \mu_{x_i}) \rangle$$
  

$$\mu_j \rangle$$
  
Mean definition:

$$\mu_{x_i} = \frac{1}{N_s} \sum_{n=1}^{N_s} x_i(n) = \langle x_i \rangle$$

## ICIRS MULTISOURCE CORRELATIVE METHODOLOGY ANALYSIS: EQUATIONS (2/2)

Measurement x from *i*-th source (MWR, NWP, RAOB ....)

 $x_i$  $a_i$ : calibration scaling of measuring system i - th $= b_i + a_i t + \varepsilon_i$  $b_i$ : calibration bias of measuring system i - th

*t*: *unobserved truth* which is common to all the measuring systems

#### Assumptions

 $\mathcal{E}_i$ : *random error* of system i - th

Assumption1 (A1). Linearity: eq. (1) holds.

<u>Assumption2 (A2)</u>:  $\varepsilon_i$  is zero average random error.

<u>Assumption3 (A3)</u>: Error orthogonality, i.e.  $\langle \varepsilon_i t \rangle = 0$ .

<u>Assumption4 (A4)</u>: Error independence i.e.:  $e_{ij} = \langle \varepsilon_i \ \varepsilon_j \rangle = 0$  with  $i \neq j$ 

<u>Assumption5 (A5)</u>: Stationarity of both t and  $x_i$ 

<u>Assumption6 (A6)</u>: the three measuring systems,  $x_i$ , i = 1, 2, 3 must observe the same quantity t.

# Outcomes Error variances

$$\begin{aligned} \hat{\sigma}_{\varepsilon_{1}}^{2} &= \sigma_{x_{1}}^{2} - \frac{c_{13}}{c_{23}}(C_{12} - e_{12}) \\ \hat{\sigma}_{\varepsilon_{2}}^{2} &= \sigma_{x_{2}}^{2} - \frac{c_{23}}{c_{13}}(C_{12} - e_{12}) \end{aligned} \qquad \begin{array}{l} \text{If calibration parameters of system 1, } a_{1}, \ b_{1}, \text{ are known} \\ \hat{\sigma}_{\varepsilon_{3}}^{2} &= \sigma_{x_{3}}^{2} - C_{13} \ C_{23}\left(\frac{1}{C_{12} - e_{12}}\right) \end{aligned}$$

#### **Calibration parameters**

$$\hat{a}_{2} = \frac{c_{23}}{c_{13}} a_{1} \quad ; \quad \hat{a}_{3} = \frac{c_{23}}{(c_{12} - e_{12})} a_{1}$$
$$\hat{b}_{2} = \langle x_{2} \rangle - \frac{c_{23}}{c_{13}} \langle x_{1} \rangle + \frac{c_{23}}{c_{13}} b_{1};$$
$$\hat{b}_{3} = \langle x_{3} \rangle - \frac{c_{23}}{(c_{12} - e_{12})} \langle x_{1} \rangle + \frac{c_{23}}{(c_{12} - e_{12})} b_{1}$$



## MULTISOURCE CORRELATIVE METHODOLOGY ANALYSIS: ERROR CORRELATION TERMS

#### **Error variances**

Error covariance e<sub>12</sub>

 $\hat{\sigma}_{\varepsilon_{1}}^{2} = \sigma_{x_{1}}^{2} - \frac{c_{13}}{c_{23}}(C_{12} - e_{12})$   $\hat{\sigma}_{\varepsilon_{2}}^{2} = \sigma_{x_{2}}^{2} - \frac{c_{23}}{c_{13}}(C_{12} - e_{12})$   $\hat{\sigma}_{\varepsilon_{3}}^{2} = \sigma_{x_{3}}^{2} - C_{13}C_{23}\left(\frac{1}{C_{12} - e_{12}}\right)$ 

- $e_{12} = \langle \varepsilon_1 \ \varepsilon_2 \rangle = \rho_{12} \ \sigma_{\varepsilon_1} \ \sigma_{\varepsilon_2}$
- $ho_{12}$ : correlation term

The term  $e_{12}$  describe the degree of error correlation between system 1 and 2 (RS and NWP for example)  $e_{12}$  is generally unknow. Any indication of its value allow to completely characterize the terms  $\hat{\sigma}_{\varepsilon_i}^2$ 

- In the special case of RS and NWP, they share the same RTE to produce the BT. Consequently, we can assume their errors perfectly correlated (i.e.  $\rho_{12}=1$ ) and of the same magnitude (i.e.  $\sigma_{\varepsilon_1} = \sigma_{\varepsilon_2} = \sigma_{\varepsilon_{RTE}}$ ).
- Thus,  $e_{12}$  reduces to  $\sigma_{\varepsilon_{RTE}}^2$ . The if we know the the error variance introduced by RTE we can estimate,  $e_{12}$  and refer to MCMA performance cases with no error correlations (upper panels)



## MULTI-SOURCE CORRELATIVE METHODOLOGY ANALYSIS

#### MCM analysis input:

From Step-V output (Qt=2)

BT\_RS (for each frequency and for each match-up); BT\_NVVP(for each frequency and for each match-up); BT\_SAT(for each frequency and for each match-up);

#### MCMconfig.ini

scaling calibration	bias calibration	error covariance
parameter for RS reference	parameter for <b>RS</b>	between RS and
system	reference system	NWP
<pre>al=l (default) gain is assumed to be normalized to I by GRUAN compensation processing s_al=0 (default) (error SD of al,TBD)</pre>	<pre>bl=0 (default) bias calibration parameter. It is assumed to be compensated by GRUAN processing s_bl=0 (default) (error SD of bl TBD)</pre>	el2=0 (default)

#### MCM analysis output:

- error standard deviations for RS/SAT/NWP
- calibration parameters for SAT/NWP only